

Karnaugh Maps: Simplify the Boolean Function

(Practice Exercise 3.6 - textbook notation example)

$F(w,x,y,z) = \Sigma(0,2,4,6,8,10,11)$ <-means put 1's in grid filling with binary pattern from a truth table.

	$y'z'$	$y'z$	yz	yz'
$w'x'$	0	1	3	2
$w'x$	4	5	7	6
wx	12	13	15	14
wx'	8	9	11	10

wx row, yz column

$w'x'y'z'$	0000	0
$w'x'y'z$	0001	1
$w'x'y'z'$	0010	2
$w'x'y'z$	0011	3
$w'x'yz'$	0100	4
$w'x'yz$	0101	5
$w'xyz'$	0110	6
$w'xyz$	0111	7
$wx'y'z'$	1000	8
$wx'y'z$	1001	9
$wx'yz'$	1010	10
$wx'yz$	1011	11
$wxy'z'$	1100	12
$wxy'z$	1101	13
$wxyz'$	1110	14
$wxyz$	1111	15

Same ordering as above	$y=0, z=0$	$y=0, z=1$	$y=1, z=1$	$y=1, z=0$
$w=0, x=0$	1	0	0	1
$w=0, x=1$	1	0	0	1
$w=1, x=1$	0	0	0	0
$w=1, x=0$	1	0	1	1

Then, use 1's Grouping Rules on the grid:

Same ordering as above	$y=0, z=0$	$y=0, z=1$	$y=1, z=1$	$y=1, z=0$
$w=0, x=0$	1	0	0	1
$w=0, x=1$	1	0	0	1
$w=1, x=1$	0	0	0	0
$w=1, x=0$	1	0	1	1

Simplified using K-map: $x'z' + w'z' + wx'y$